

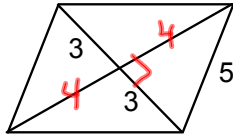
1. The area of a triangle is 48 units<sup>2</sup>.  
The height is 8 units. What is the  
base? 12u

$$A = \frac{1}{2}bh$$

$$48 = \frac{1}{2} \cdot 8 \cdot b$$

2. 2nd diagonal 8  
Area  $\frac{1}{2} \cdot 8 \cdot 6 = 24u^2$

Rhombus



$$5^2 = 3^2 + x^2$$

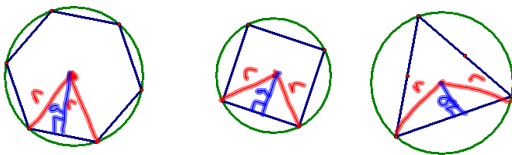
$$16 = x^2$$

$$4 = x$$

Any regular polygon can be  
inscribed in a circle.

Radius--from center to vertex

Apothem--from the center and perpendicular to one side



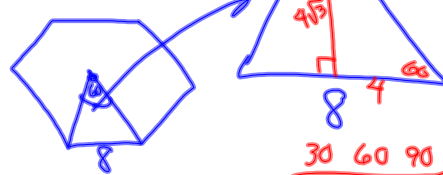
$$A = \frac{1}{2} a \cdot p$$

perimeter

## 11-3 Areas of Regular Polygons and Circles

Area =  $\frac{1}{2} a p$

example 1:  
regular hexagon  
side = 8 cm



$$360 \div 6 = 60^\circ$$

$$\frac{30}{9} \quad \frac{60}{4\sqrt{3}} \quad \frac{90}{4\sqrt{3}}$$

$$A = \frac{1}{2} 4\sqrt{3} \cdot 48$$

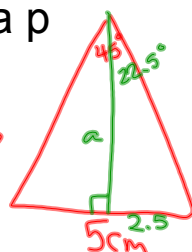
$$96\sqrt{3} \text{ cm}^2$$

Area =  $\frac{1}{2} a p$

example 2:  
regular octagon  
side = 5 cm



$$360 \div 8 = 45$$



$$\tan 22.5 = \frac{2.5}{a}$$

$$a \tan 22.5 = 2.5$$

$$a = \frac{2.5}{\tan 22.5}$$

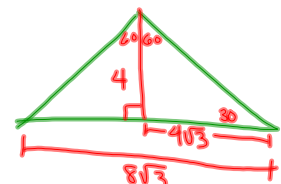
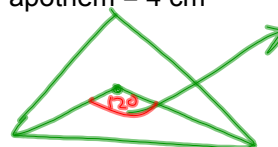
$$a \approx 6.04$$

$$A = \frac{1}{2} (6.04) 40$$

$$\approx 120.7 \text{ cm}^2$$

Area =  $\frac{1}{2} a p$

example 3:  
regular triangle  
apothem = 4 cm



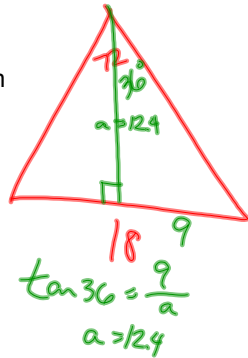
$$P = 24\sqrt{3}$$

$$A = \frac{1}{2} 4 \cdot 24\sqrt{3}$$

$$= 48\sqrt{3} \text{ cm}^2$$

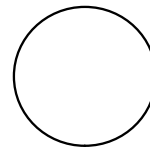
$$\text{Area} = \frac{1}{2} a p$$

example 4:  
regular pentagon  
perimeter = 90 cm  
one side = 18



$$A = 557.4 \text{ cm}^2$$

$$\text{Area of a circle} = \pi r^2$$



$$r = 4 \text{ cm}$$

$$A = 16\pi \text{ cm}^2$$

$$C = 24\pi$$

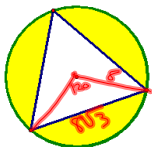
$$r = 12$$

$$A = 144\pi \text{ cm}^2$$

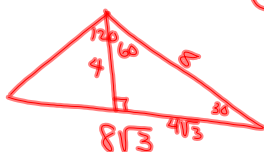
Find the area of the shaded region.  
The radius is 8 cm.



$$\begin{aligned} A_{\text{circle}} - A_{\text{sq}} \\ 64\pi - (8\sqrt{2})^2 \\ 64\pi - 128 \\ 73.1 \text{ cm}^2 \end{aligned}$$



Find the area of the shaded region.  
One side of the triangle is  $8\sqrt{3}$  cm.



$$\begin{aligned} A_{\text{circle}} - A_{\Delta} \\ 64\pi - \frac{1}{2} 4 \cdot 24\sqrt{3} \\ 64\pi - 48\sqrt{3} \\ 117.9 \text{ cm}^2 \end{aligned}$$

HW

p613-614

8-14, 16, 30

Find the area of each polygon. Round to the nearest tenth.

8. a regular octagon with a perimeter of 72 inches
9. a square with a perimeter of  $84\sqrt{2}$  meters
10. a square with apothem length of 12 centimeters
11. a regular hexagon with apothem length of 24 inches
12. a regular triangle with side length of 15.5 inches
13. a regular octagon with side length of 10 kilometers

Find the area of each shaded region. Assume that all polygons that appear to be regular are regular. Round to the nearest tenth.

14.



16.



Find the area of each circle. Round to the nearest tenth.

30.  $C = 34\pi$